

Measures of Association

- Assess the size (strength) of the relationship between exposure (potential “cause”) and outcome (“disease”)
 - Re: statistical tests are about the “significance” of association
 - They are not used to indicate the magnitude of the effect
 - They are about the likelihood that the size of the difference observed was due to chance given that the null hypothesis is true

- Compare:
 - Disease frequency in exposed v. Disease frequency in non-exposed
- Or:
 - Odds of exposure in those with disease (cases) and those without the disease (controls)

Risk Data

		Disease/Outcome	
		present	absent
Risk Factor	Present (exposed)	a	b
	Absent (not exposed)	c	d

Incidence Rate Data

	exposed	Non-exposed	Total
	Number of cases	a	b
Case-time at risk	c	d	c+d

3 common measures

- Risk ratio(Relative Risk)
 - Incidence rate ratio
 - Odds ratio
- All a ratio of 2 estimates of Dz frequency

Risk Ratio (Relative Risk)

- Risk of Dz in exposed to risk of Dz in non-exposed
- $RR = P(D+ | E+) / P(D+ | E-)$
- Not for use in case-control studies b/c D+ is arbitrarily defined by the number of cases included in the study

		Disease	
		present	absent
Risk Factor	present	a	b
	absent	c	d

$a / (a + b) = dz$
w/ factor

$c / (c + d) = dz$
w/OUT factor

RR = $(a / (a+b)) / (c / (c+d))$

> 1 = increased disease due to factor, < 1 = protection due to factor, =1 ~ exposure has no effect

Or use: https://www.medcalc.org/calc/relative_risk.php

Or use: something else

Example

- Risk Factor = FPT
- Disease = Scours
- Sampled 12 calves with refractometer
- 5 calves < 5.5 g/dl
- 7 calves > 5.5 g/dl
- 4 calves had scours
- 8 calves did not scour
- 3 had FPT and scours
- **Is there a strong association between FPT and scours?**

Disease =
present Scours absent

$a / (a + b) =$
dz w/ factor

$c / (c + d) =$
dz w/OUT factor

R R = $(a / (a+b)) / (c / (c+d))$

$(3/5) / (1/7) = \underline{\quad}$; Those calves with FPT are $\underline{\quad}$ times more likely to scour

OR:

Incidence Rate Data

	Disease	
	# of cases	Animal time at risk
Present (exposed)	a	b
Risk Factor		
Absent (not exposed)	c	d

Incidence Rate Data

- $IR = (a/b) / (c/d)$
- Ranges from 0 to infinity
- 1 means no association
- >1 means increased rate of dx with exposure
- <1 means protective exposure

Incidence Rate example

	Disease	
	# mast cases	Animal time at risk
Present (no dip)	18	250
Risk Factor		
Absent (dip)	8	236

$IR = (18/250) / (8/236) = 2.12 \rightarrow$ rate of mast 2.1
 higher in cows not pre-dipped

Odds Ratio

		Disease	
		present	absent
Risk Factor	Present (exposed)	a	b
	Absent (not exposed)	c	d

Odds Ratio

- Odds of disease in exposed group divided by odds of disease in non-exposed group
- $OR = \text{odds } (D+|E+) / \text{odds } (D+|E-)$
 - $= (a/b) / (c/d)$
 - $= (a*d) / (b*c)$
- Can also be calculated as $(E+|D+) / (E+|D-)$
- Interpret the same as RR

Odds Ratio

- Can "switch" exposure and disease
- OR is used for Case-Control studies b/c disease frequency is "artificially" established

Relationship

- If disease occurs rarely in population (e.g. risk is ~4%) $OR \sim RR$
- If disease occurrence is large, $OR > IR > RR$ for same measurement

Confidence intervals (CI)

- CI reflect the level of uncertainty (precision) in a point estimate
- Indicate the range of expected values
- Conveys more information than the point estimate and a p-value
 - Clearly shows a range of likely values for the population parameter

Confidence intervals (CI)

- Ex: for 95% CI:
 - Repeat study measurements an infinite number of times and make 95% CI for each one, 95% of these would include the TRUE parameter value
- If 95% CI includes null value (e.g. RR=1), it ***suggests*** the parameter is not statistically different from the null at a p-value of 0.05
 - It is not a hypothesis test though!